

Math Field Day 2023

Mad Hatter 6-8

CSU Fresno

www.fresnostate.edu/csm/math/

15 April 2023

Mad Hatter 6-8

Math Field
Day 2023

CSU Fresno

Welcome to Fresno State!

The Mad Hatter Marathon is a competition in rapid computation and problem solving. You will find that you do not have time to solve every problem. After a few minutes you may feel “mentally out of breath.” Do not let this discourage you. Your fellow contestants feel the same way. That is why this contest is called *Mad Hatter Marathon!*

Mad Hatter 6-8

Math Field
Day 2023

CSU Fresno

The Mad Hatter Marathon is divided into two problem solving periods, each lasting 45 minutes. Between the two periods there will be a 15 minute break.

Part I

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

- **This part of the exam consists of 30 problems.**
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Part I

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

- This part of the exam consists of 30 problems.
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Part I

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

- This part of the exam consists of 30 problems.
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Part I

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

- This part of the exam consists of 30 problems.
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Part I

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

- This part of the exam consists of 30 problems.
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Part I

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

- This part of the exam consists of 30 problems.
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Rules and Scoring

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

You may use pencil and scratch paper to do calculations, but **calculators are not allowed**.

Your score is the total number of correct answers, so give the best answer that you can in the time available for each problem. There is no penalty for guessing.

Reminders

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

- Please turn off any devices that could make noise, such as cell phones, beepers, watches, etc.
- If your pencil breaks or needs sharpening, stay in your seat and raise your hand.
- Keep your eyes on your own paper. Keep your Scantron flat on your desk. Contestants caught cheating will be disqualified.

Ready... Set... Go!

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Prepare to begin the *Mad Hatter Marathon!*

Part I - Problem 1

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

Which of the following rectangles is *impossible*?

Rectangle	A	B	C	D	E
Area (in m^2)	25	25	16	16	9
Perimeter (in m)	29	20	16	20	9

- A Rectangle A
- B Rectangle B
- C Rectangle C
- D Rectangle D
- E Rectangle E

Part I - Problem 2

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

During the Mario Kart Circuit, Luigi drove at an average speed of 70 mph for the first 30 minutes. For the next 20 minutes, Luigi had an average speed of 40 mph. During the final 10 minutes, Luigi's average speed was 60 mph. What was Luigi's average speed (in mph) for the entire hour?

A $54.\overline{3}$

B $56.\overline{6}$

C $58.\overline{3}$

D 60

E $62.\overline{6}$

Part I - Problem 3

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

What is the area of an equilateral triangle with side length 2 units?

A $\frac{3\sqrt{3}}{2}$

B 2

C $2\sqrt{2}$

D $2 + \sqrt{2}$

E $\sqrt{3}$

Part I - Problem 4

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

The five starting players on the Funky Dunkers basketball team have heights (in feet and inches)

$4'11''$

$5'4''$

$5'8''$

$5'8''$

$5'11''$

What is the mean height of the starting five players?
(Remember that $12'' = 1'$.)

A $5'4''$

B $5'5''$

C $5'6''$

D $5'7''$

E $5'8''$

Part I - Problem 5

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

Which of the following statements is FALSE?

- A Any two circles are similar.
- B Any two squares are similar.
- C Any two rectangles are similar.
- D Any two spheres are similar.
- E Any two cubes are similar.

Part I - Problem 6

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

There are 15 cats and 11 dogs in a math class. If an animal is selected at random to get a treat, what is the probability that a dog will be selected?

A $\frac{4}{26}$

B $\frac{11}{26}$

C $\frac{11}{15}$

D $\frac{15}{11}$

E $\frac{26}{11}$

Part I - Problem 7

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

Tom Nook makes a profit of 5 Bells for each wallpaper he sells, 2 Bells for each tool he sells, and $\frac{1}{2}$ Bell for each flower he sells. Today he sold 7 items and made a profit of 17 Bells. Assuming he sold at least one of each item type, which of the following statements must be TRUE?

- A Tom sold an odd number of flowers.
- B Tom sold an even number of tools.
- C Tom sold an odd number of wallpapers.
- D Tom sold more wallpapers than tools.
- E Tom sold the same number of flowers as wallpapers.

Part I - Problem 8

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

Chewbacca travels 48 inches with each stride. Leia moves 24 inches with each of her strides. If Chewbacca and Leia each start walking along a 1 mile path and both take the same number of strides, how many feet behind will Leia be when Chewbacca completes the mile?

A 1663

C 3298

E 5280

B 2640

D 3616

Part I - Problem 9

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

A string has been cut into 4 pieces, all of different lengths. The length of each piece is 2 times the length of the next smaller piece. What fraction of the original string is the longest piece?

A $\frac{8}{15}$

B $\frac{2}{5}$

C $\frac{1}{2}$

D $\frac{6}{13}$

E $\frac{5}{8}$

Part I - Problem 10

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

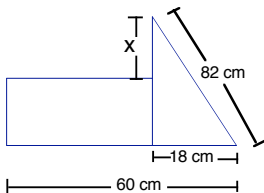
Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

In the picture below, if the area of the rectangle is 2688 cm^2 then what is the length X ?



A 16 cm

C 26 cm

E 54 cm

B 9 cm

D 42 cm

Part I - Problem 11

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

We sold 380 tickets to this weekend's butter churning competition. That was 25% more than we sold last year. How many tickets did we sell last year?

A 304

B 285

C 95

D 190

E 250

Part I - Problem 12

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

A store had a sale on t-shirts: for every two t-shirts purchased at the regular price, a third t-shirt would cost \$1. If Tom bought twelve t-shirts for \$120.00, what was the regular price for one t-shirt?

A \$10.00

C \$13.50

E \$15.00

B \$12.00

D \$14.50

Part I - Problem 13

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

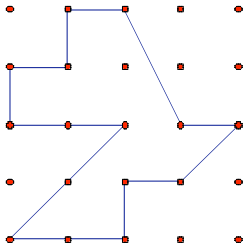
Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

If the dots are spaced one unit apart then what is the area (in square units) of the pictured polygon?



A 6.5

B 7.0

C 7.5

D 8.0

E 8.5

Part I - Problem 14

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Problem 7

Problem 8

Problem 9

Problem 10

Problem 11

Problem 12

Problem 13

Problem 14

Part I:
Problems
16-30

When you convert the base ten number 2023 into base 5, what will be the digit in the units place?

A 1

B 2

C 3

D 4

E 0

Part I - Problem 15

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

Problem 27

Problem 28

Problem 29

Problem 30

What is the smallest positive integer $x > 100$ such that every number formed by rearranging the digits of x is prime?

A 101

B 103

C 113

D 117

E 127

Part I - Problem 16

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

Problem 27

Problem 28

Problem 29

Problem 30

Bulbasaur, Charizard, and Snorlax just finished playing a video game. Bulbasaur scored 5,450 points, Charizard got 70% of Bulbasaur's score, and Snorlax finished with 200% of Charizard's score. What percent of Bulbasaur's score was Snorlax's score?

- A 140% B 150% C 85% D 130% E 120%

Part I - Problem 17

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

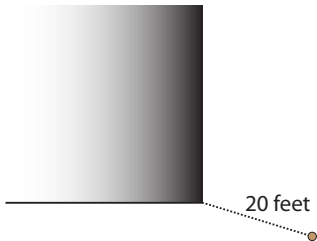
Problem 27

Problem 28

Problem 29

Problem 30

Snuffles the dog is tied to the corner of a square building by a 20 foot leash as shown. What is the total area (in square feet) that Snuffles is able to roam?



A 100π

C $100\sqrt{3}\pi$

E 400π

B $100\sqrt{2}\pi$

D 300π

Part I - Problem 18

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

Problem 27

Problem 28

Problem 29

Problem 30

If the coordinates of three vertices of a parallelogram are

$$A(1, 1), \quad B(2, 4), \quad \text{and} \quad C(-5, 1)$$

then what is the area of the parallelogram?

A 36

B 48

C 72

D 9

E 18

Part I - Problem 19

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

Problem 27

Problem 28

Problem 29

Problem 30

For a cube, how many different paths are there from one corner to the opposite corner that travel along exactly three edges?

A 1

B 3

C 6

D 8

E 12

Part I - Problem 20

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

Problem 27

Problem 28

Problem 29

Problem 30

If $n! = 1 \cdot 2 \cdot 3 \cdot 4 \cdots n$ then the ones digit of the number

$1! + 2! + 3! + \cdots + 2023!$ is ...

- A 1
- B 3
- C 5
- D 9
- E None of these

Part I - Problem 21

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

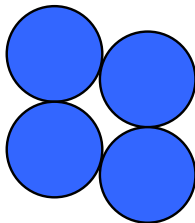
Problem 27

Problem 28

Problem 29

Problem 30

Four identical circles are touching as shown. What is the shape whose vertices are the centers of the circles?



- A trapezoid
- B square
- C rectangle
- D kite
- E rhombus

Part I - Problem 22

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

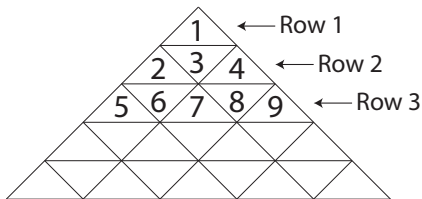
Problem 27

Problem 28

Problem 29

Problem 30

If the pattern continues which row will contain the number 2023 ?



A 27

B 35

C 37

D 45

E 53

Part I - Problem 23

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

Problem 27

Problem 28

Problem 29

Problem 30

If a circle is inscribed in a right triangle with legs 6 and 8 then what will be the radius of the circle?

- A $\sqrt{2}$
- B 2
- C $\sqrt{3}$
- D 3
- E None of these

Part I - Problem 24

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

Problem 27

Problem 28

Problem 29

Problem 30

If you add up the first one hundred positive odd integers

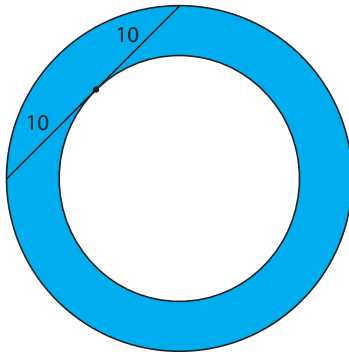
$$1 + 3 + 5 + 7 + \text{ninety-six more numbers...}$$

what do you get?

- A 10,000
- B 10,100
- C 9,990
- D 9,900
- E 9,998

Part I - Problem 25

The line is 20 units long and tangent to the inner circle.
What is the area (in square units) of the blue region?



A 20π

B $20\sqrt{2}\pi$

C 50π

D $50\sqrt{2}\pi$

E 100π

Part I - Problem 26

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

Problem 27

Problem 28

Problem 29

Problem 30

Suppose that $x + y = 3$ and $x^2 + y^2 = 7$. Then

$$x^4 + y^4 = \dots$$

A 49

B 51

C 45

D 64

E 47

Part I - Problem 27

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

Problem 27

Problem 28

Problem 29

Problem 30

A rectangle has perimeter 10 and diagonal $\sqrt{15}$. What is its area?

A 5

B 10

C 15

D 20

E 25

Part I - Problem 28

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

Problem 27

Problem 28

Problem 29

Problem 30

A circle expands outward and its circumference increases by 20%. By what percent does the area increase?

A 20%

C 40%

E None of
these

B 22%

D 44%

Part I - Problem 29

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

Problem 27

Problem 28

Problem 29

Problem 30

A serving size of Grandpa Joe's Ketchup Soda is 225 milliliters. If Wallace buys a 2 liter bottle of the soda then how many servings will Wallace have?



A 80/9

B 18

C $15/2$

D 12

E None of these

Part I - Problem 30

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

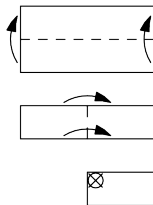
Problem 27

Problem 28

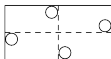
Problem 29

Problem 30

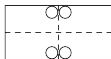
A rectangular piece of paper is folded in half from bottom to top, and then folded again from left to right as shown. A hole is punched in the upper left corner of the folded paper as shown. What will the punched paper look like when it is unfolded?



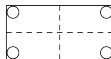
(A)



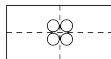
(B)



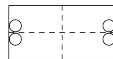
(C)



(D)



(E)



Mad Hatter - 15 minute break

Math Field
Day 2023

CSU Fresno

Part I

Part I:
Problems 1-15

Part I:
Problems
16-30

Problem 15

Problem 16

Problem 17

Problem 18

Problem 19

Problem 20

Problem 21

Problem 22

Problem 23

Problem 24

Problem 25

Problem 26

Problem 27

Problem 28

Problem 29

Problem 30

Whew! You've reached the end of Part I.

- Please make sure your full name and school name are on your Scantron form.
- Pass your Scantrons in.
- You may leave your belongings here during the break.
- Part II will begin in **15 minutes**.

Mad Hatter - Part II

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

The End

The rules for this part of the competition are the same as the previous part.

- This part of the exam consists of 30 problems.
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Mad Hatter - Part II

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

The End

The rules for this part of the competition are the same as the previous part.

- This part of the exam consists of 30 problems.
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Mad Hatter - Part II

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

The End

The rules for this part of the competition are the same as the previous part.

- This part of the exam consists of 30 problems.
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Mad Hatter - Part II

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

The End

The rules for this part of the competition are the same as the previous part.

- This part of the exam consists of 30 problems.
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Mad Hatter - Part II

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

The End

The rules for this part of the competition are the same as the previous part.

- This part of the exam consists of 30 problems.
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Mad Hatter - Part II

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

The End

The rules for this part of the competition are the same as the previous part.

- This part of the exam consists of 30 problems.
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Mad Hatter - Part II

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

The End

The rules for this part of the competition are the same as the previous part.

- This part of the exam consists of 30 problems.
- The problems will be shown one at a time.
- You will have ninety seconds to solve the problem shown.
- After ninety seconds a new problem will be shown.
- You may move to a new question without solving the old one.

As soon as you have solved the problem mark your answer in the corresponding space on the Scantron form.

Ready... Set... Go!

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

The End

Prepare to restart the *Mad Hatter Marathon!*

Part II - Problem 1

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

Crazy Dave chews two packs of Meatball Bubble Gum every day. If each package of gum costs \$2.25 then how much will Dave spend on the gum this year?



A \$1534.50

B \$1539.00

C \$1642.50

D \$1647.00

E None of these

Part II - Problem 2

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

Lando always wears pants, shirt and a cape (even to bed!) If he has eight different pants, eleven different shirts and three different capes, how many different ensembles can he wear?



A 22

B 82

C 174

D 188

E 264

Part II - Problem 3

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

Steve's farm of mutant animals has three-legged dingoes and five-legged wallabees. If in one pen, his toddler counts 83 legs and 23 heads, how many wallabees are in the pen?

- A 7
- B 9
- C 12
- D 16
- E 17

Part II - Problem 4

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

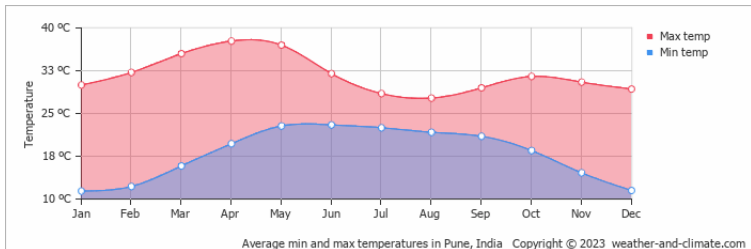
Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

The graph shows the average daily high and low temperatures for each month. During which month is the sum of the average daily high and low temperatures the largest?



- A April
- B May

- C July
- D August

- E September

Part II - Problem 5

Neytiri has one of each type of coin in her pocket. If two coins are taken out at random what is the probability that the total will be greater than 40 cents?



A 30%

B $33.\bar{3}\%$

C 50%

D 60%

E $66.\bar{6}\%$

Part II - Problem 6

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

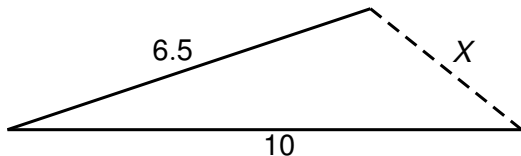
Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

Which of the following is the smallest whole number that could be the length x ?



A 3

B 4

C 5

D 6

E 7

Part II - Problem 7

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

Round to two decimal places:

$$\sqrt{10} + \sqrt{10} + \sqrt{10} + \sqrt{10} + \sqrt{10} - \sqrt{50}$$

A 14.61

C 10.76

E 0.00

B 12.93

D 8.74

Part II - Problem 8

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

If \clubsuit is a non-zero real number then which of the following must be negative?

A $-\clubsuit$

B $-\frac{\clubsuit}{\clubsuit}$

C $-\clubsuit^3$

D All of the above must be negative

E None of the above must be negative

Part II - Problem 9

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

Evaluate

$$20 - (3 \times 2^3 - 5).$$

- A -191
- B 1
- C 11
- D 131
- E None of these

Part II - Problem 10

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

What is the mean number of letters in the English words for the first ten counting numbers?

ONE TWO THREE FOUR ... TEN

- A 3.3
- B 3.5
- C 3.7
- D 3.9
- E 4.1

Part II - Problem 11

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

If the second Saturday of a month is a one digit even number then the date of the fourth Monday of the same month will be the...

A 22nd

B 23rd

C 24th

D 25th

E 26th



Part II - Problem 12

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

How many non-congruent triangles have integer side lengths and a total perimeter of 8 units?

- A zero
- B one
- C two
- D three
- E four

Part II - Problem 13

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

Mister Bojangle's candy basket is filled with bubble gum and lollipops each of which is either cherry flavored or grape flavored.

If 20% of the candy basket is lollipops and 40% of the bubble gum is grape, then what percentage of the candy basket is cherry bubble gum?

A 40%

B 48%

C 52%

D 60%

E 66%

Part II - Problem 14

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

Problem II-14

Problem II-15

Part II:
Problems
16-30

The End

The Réaumur scale is an alternative temperature scale to the Fahrenheit scale. Suppose we have the following equivalences:

Fahrenheit	Réaumur
77	20
167	60

Assuming that Réaumur and Fahrenheit are linearly related, how many Réaumur degrees is equal to 257 degrees Fahrenheit?

A 88

B 100

C 112

D 120

E 132

Part II - Problem 15

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Problem II-1

Problem II-2

Problem II-3

Problem II-4

Problem II-5

Problem II-6

Problem II-7

Problem II-8

Problem II-9

Problem II-10

Problem II-11

Problem II-12

Problem II-13

Problem II-14

Problem II-15

Part II:
Problems
16-30

The End



During its trip to the planet Iota Geminorum, six tribbles stowed away on the Starship Enterprise.

If the population of tribbles doubles every day, in how many days will the tribble population top 2023 tribbles?

A 13

B 17

C 5

D 15

E 9

Part II - Problem 16

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

Problem II-16

Problem II-17

Problem II-18

Problem II-19

Problem II-20

Problem II-21

Problem II-22

Problem II-23

Problem II-24

Problem II-25

Problem II-26

Problem II-27

Problem II-28

Problem II-29

Problem II-30

The End

Suppose that $x > y$ and that

$$x + \frac{1}{x} = 2023 + \frac{1}{2023}$$

$$y + \frac{1}{y} = 2023 + \frac{1}{2023}$$

Which is a possible value of $x \cdot y$?

- (A) 1
- (B) $\frac{1}{2023}$
- (C) 2023
- (D) All of the above
- (E) (B) and (C) but not (A)

Part II - Problem 17

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

Problem II-16

Problem II-17

Problem II-18

Problem II-19

Problem II-20

Problem II-21

Problem II-22

Problem II-23

Problem II-24

Problem II-25

Problem II-26

Problem II-27

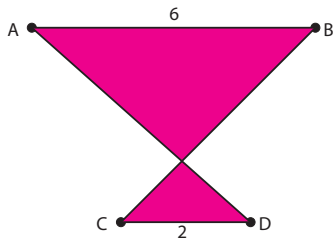
Problem II-28

Problem II-29

Problem II-30

The End

Assume that the line AB is parallel to the line CD and that the lines have the lengths shown in the figure. If the distance between AB and CD is 10, then what is the combined area of the two triangles?



- A 26 B 28 C 24 D 27 E 25

Part II - Problem 18

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

Problem II-16

Problem II-17

Problem II-18

Problem II-19

Problem II-20

Problem II-21

Problem II-22

Problem II-23

Problem II-24

Problem II-25

Problem II-26

Problem II-27

Problem II-28

Problem II-29

Problem II-30

The End

A vampire has come to town. Each month a vampire sucks blood from two humans and creates two new vampires. After 6 months how many vampires will be in town?



A 48

B 1458

C 96

D 81

E 729

Part II - Problem 19

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

Problem II-16

Problem II-17

Problem II-18

Problem II-19

Problem II-20

Problem II-21

Problem II-22

Problem II-23

Problem II-24

Problem II-25

Problem II-26

Problem II-27

Problem II-28

Problem II-29

Problem II-30

The End

Suppose that

$$y > 0$$

$$x > y$$

$$z \neq 0$$

Which of the following inequalities is NOT always true?

A $x + z > y + z$

B $x - z > y - z$

C $xz^2 > yz^2$

D $\frac{x}{z^2} > \frac{y}{z^2}$

E $xz > yz$

Part II - Problem 20

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

Problem II-16

Problem II-17

Problem II-18

Problem II-19

Problem II-20

Problem II-21

Problem II-22

Problem II-23

Problem II-24

Problem II-25

Problem II-26

Problem II-27

Problem II-28

Problem II-29

Problem II-30

The End

Imagine a room with 33 people. Suppose that 12 of the people speak Spanish, 25 people speak English, and 3 people speak *neither* Spanish nor English.

How many people in the room speak **both** Spanish and English?

A 7

B 3

C 6

D 4

E 5

Part II - Problem 21

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

Problem II-16

Problem II-17

Problem II-18

Problem II-19

Problem II-20

Problem II-21

Problem II-22

Problem II-23

Problem II-24

Problem II-25

Problem II-26

Problem II-27

Problem II-28

Problem II-29

Problem II-30

The End



A singles tennis tournament begins with 128 players. How many single-elimination games must be played to determine a champion?

A 63

C 127

E 256

B 64

D 128

Part II - Problem 22

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

Problem II-16

Problem II-17

Problem II-18

Problem II-19

Problem II-20

Problem II-21

Problem II-22

Problem II-23

Problem II-24

Problem II-25

Problem II-26

Problem II-27

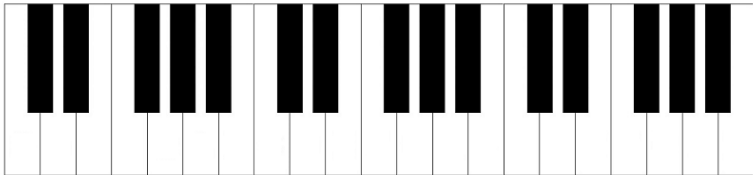
Problem II-28

Problem II-29

Problem II-30

The End

The pictured keyboard has black keys and white keys. What **percentage** of the keys are black?



- A $58.\bar{3}$ B $48.\bar{6}$ C $33.\bar{3}$ D 50 E $41.\bar{6}$

Part II - Problem 23

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

Problem II-16

Problem II-17

Problem II-18

Problem II-19

Problem II-20

Problem II-21

Problem II-22

Problem II-23

Problem II-24

Problem II-25

Problem II-26

Problem II-27

Problem II-28

Problem II-29

Problem II-30

The End

What is the **smallest** positive integer that must be added to 2023 in order to get a number that is divisible by 13?

A 1

B 2

C 3

D 4

E 5

Part II - Problem 24

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

Problem II-16

Problem II-17

Problem II-18

Problem II-19

Problem II-20

Problem II-21

Problem II-22

Problem II-23

Problem II-24

Problem II-25

Problem II-26

Problem II-27

Problem II-28

Problem II-29

Problem II-30

The End

Janet mixes her world-famous hot sauce in a cylindrical jar with a radius of 6 cm and a height of 12 cm. When the mixing jar is full, she divides the sauce into three equal portions and pours the sauce into smaller cylindrical jars that have the same height as the mixing jar.

What is the minimum radius for the smaller jars?

A $2\sqrt{3}$ cm

B $\sqrt{3}$ cm

C 4 cm

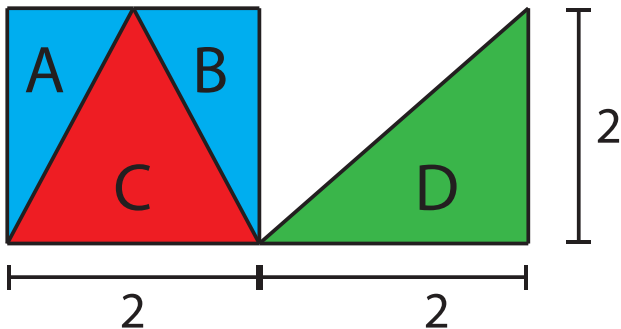
D $4\sqrt{3}$ cm

E 6 cm



Part II - Problem 25

Which amounts to the greatest area?



- A $A + B$
- B C
- C D
- D All the above have the same area

Part II - Problem 26

The odometer currently reads 304395 miles. How many miles must be driven before all the digits are different?



- A** 117 **B** 124 **C** 152 **D** 168 **E** 228

Part II - Problem 27

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

Problem II-16

Problem II-17

Problem II-18

Problem II-19

Problem II-20

Problem II-21

Problem II-22

Problem II-23

Problem II-24

Problem II-25

Problem II-26

Problem II-27

Problem II-28

Problem II-29

Problem II-30

The End

If the measures, in degrees, of the three angles of a triangle are x , $x + 10$, and $2x - 6$, the triangle must be...

- A right.
- B equilateral.
- C isosceles.
- D scalene.

Part II - Problem 28

How many times faster does the second hand of a clock move than the hour hand of the clock?



A 240

B 600

C 720

D 1440

E 3600

Part II - Problem 29

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

Problem II-16

Problem II-17

Problem II-18

Problem II-19

Problem II-20

Problem II-21

Problem II-22

Problem II-23

Problem II-24

Problem II-25

Problem II-26

Problem II-27

Problem II-28

Problem II-29

Problem II-30

The End

What is the sum of all of the numbers in the table?

16	5	9	4
3	10	6	15
2	11	7	14
13	8	12	1

A 118

B 124

C 136

D 156

E 164

Part II - Problem 30

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

Problem II-16

Problem II-17

Problem II-18

Problem II-19

Problem II-20

Problem II-21

Problem II-22

Problem II-23

Problem II-24

Problem II-25

Problem II-26

Problem II-27

Problem II-28

Problem II-29

Problem II-30

The End

How many positive integer numbers are equal to exactly twice the sum of their digits?

- A None
- B One number
- C Two numbers
- D Three numbers
- E Infinitely many numbers

Mad Hatter - Done!

Math Field
Day 2023

CSU Fresno

Part II

Part II:
Problems 1-15

Part II:
Problems
16-30

The End

You made it!

- Please make sure your full name and school name are on your Scantron form.
- Pass your Scantron in.
- Please take your belongings with you.
- There will be games and other fun activities in Science II, Room 308, from 1:00-2:30.
- The awards ceremony will be in the Science II courtyard beginning at **2:45pm**. If there are any ties, you have to be present to win the tiebreaker. See you there!

Part I

1	E	6	B	11	A	16	A	21	E	26	E
2	C	7	E	12	D	17	D	22	D	27	A
3	E	8	B	13	C	18	E	23	B	28	D
4	C	9	A	14	C	19	C	24	A	29	A
5	C	10	A	15	C	20	B	25	E	30	B

Part II

1	C	6	B	11	C	16	A	21	C	26	A
2	E	7	D	12	B	17	E	22	E	27	D
3	A	8	B	13	B	18	E	23	E	28	C
4	B	9	B	14	B	19	E	24	A	29	C
5	D	10	D	15	E	20	A	25	D	30	B